



ANALYTICAL STUDY ON TENSILE STRENGTH OF CURVED FRP REINFORCEMENT

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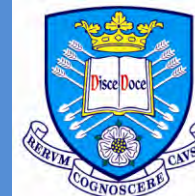
OUTLINE



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- **Introduction**
- **Performance of curved FRP's**
- **Experimental Programme/ Results**
- **Analytical study**
- **Conclusions**

Introduction

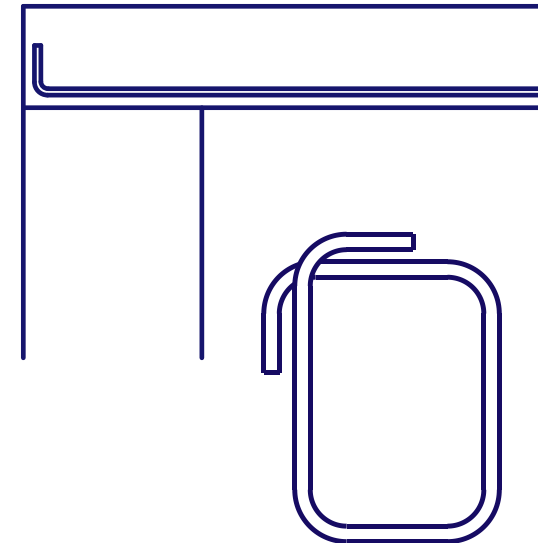


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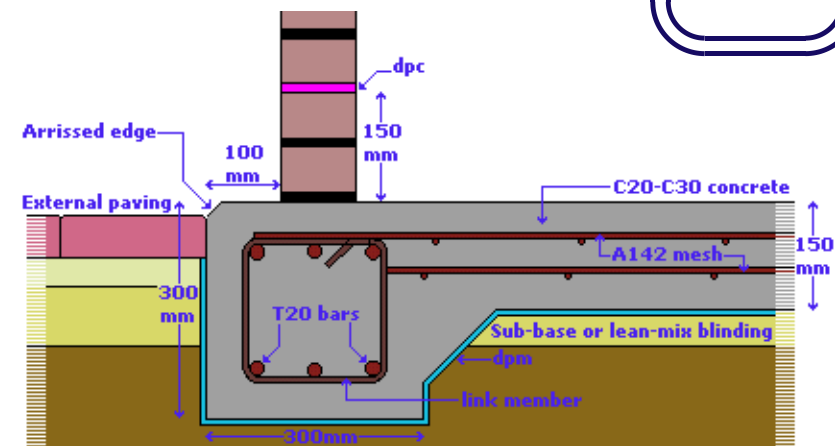
- End anchorages



- Element connection



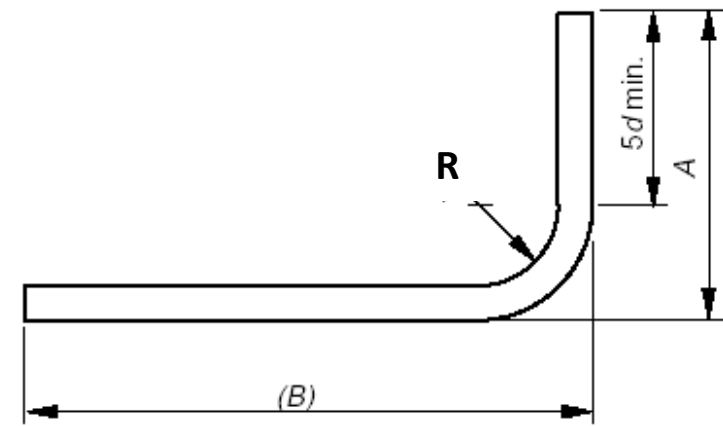
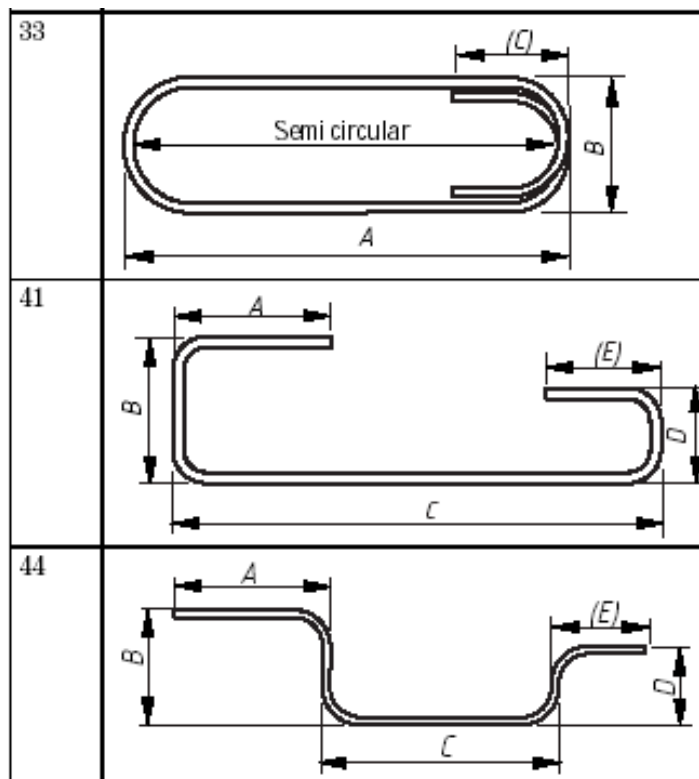
- Shear reinforcement



Introduction



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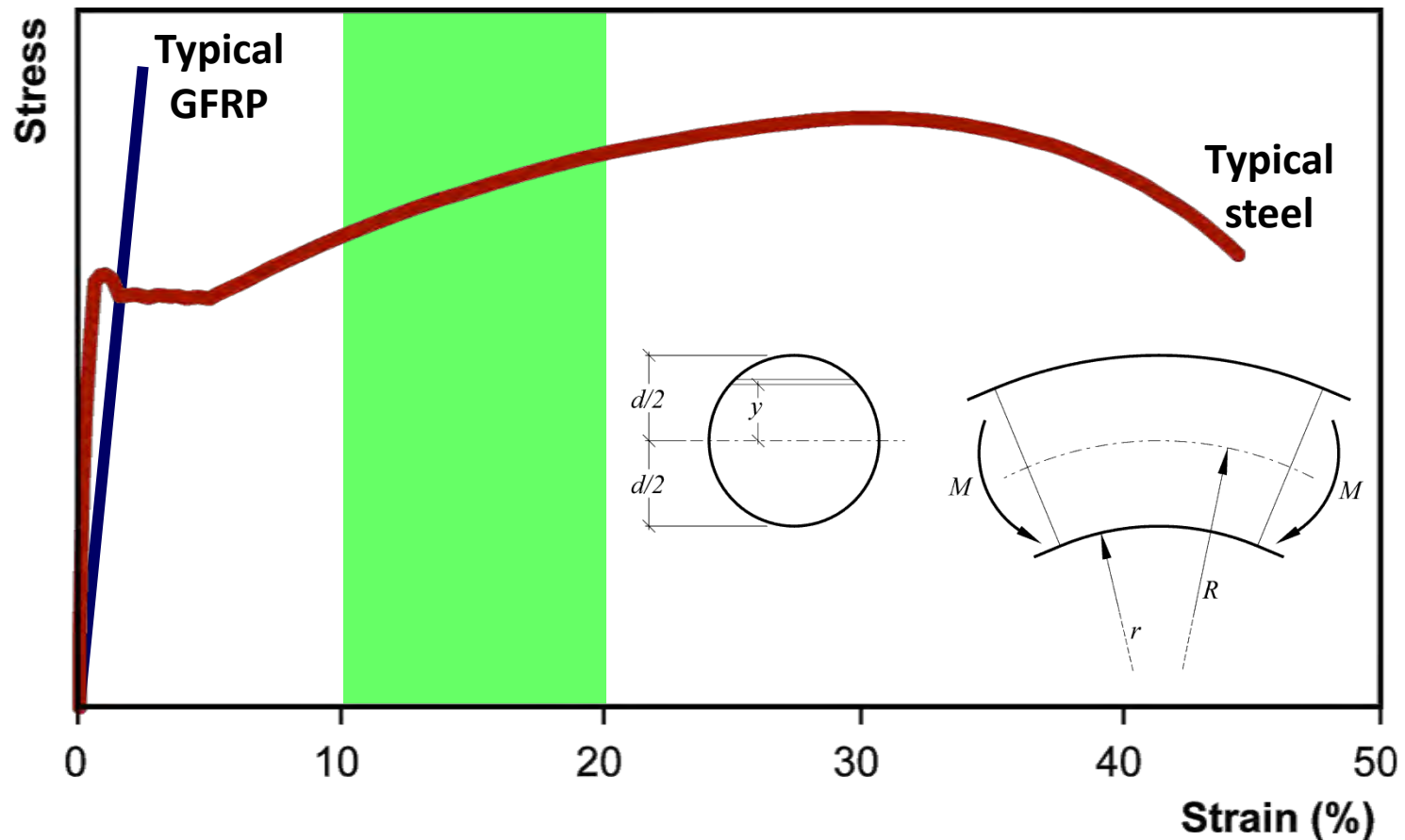
$$R \geq 2d$$

Standardised shapes (BS 8666)

Plastic strain induced by bending



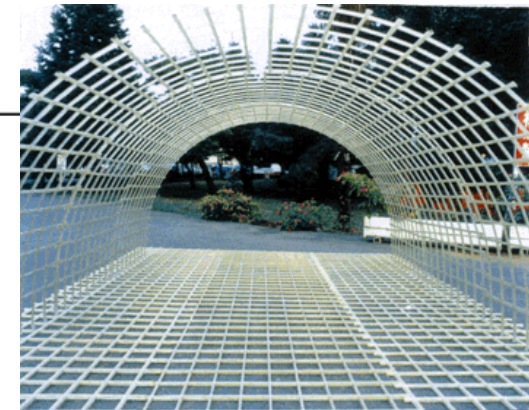
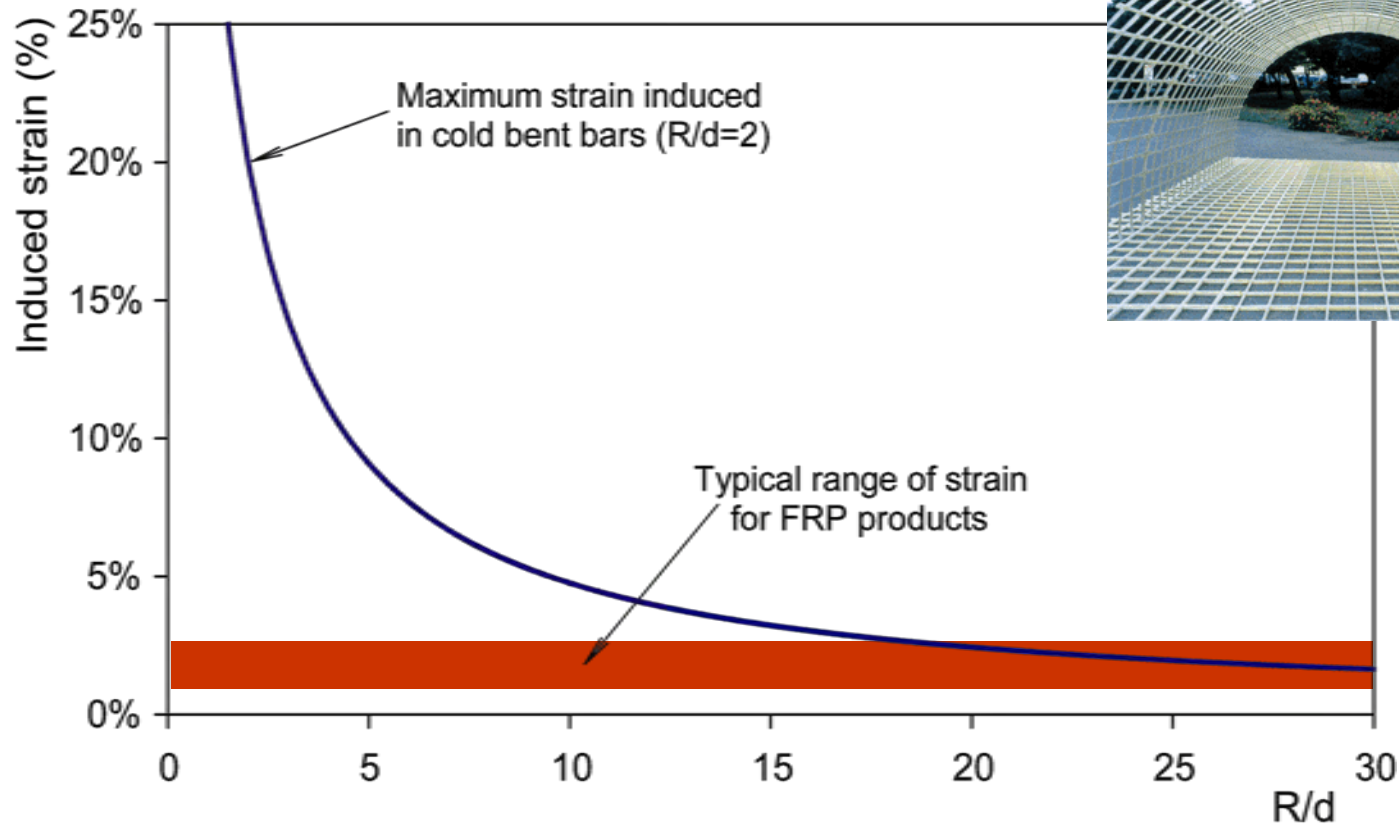
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Cold bending of FRP's



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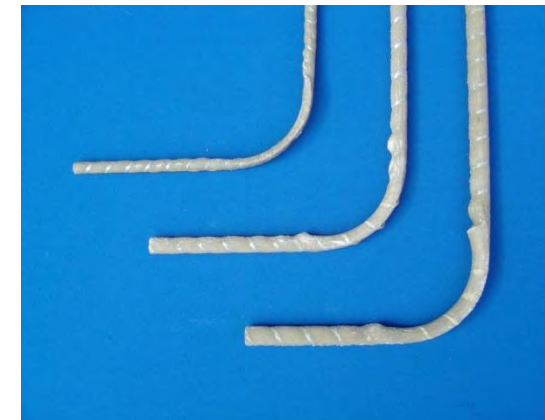


Pre-bent FRP's



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- **Thermosetting FRP's:**
can only be pre-bent at the
factory
- **Thermoplastic FRP's:**
could offer a valid solution
for on-site bending of
reinforcement

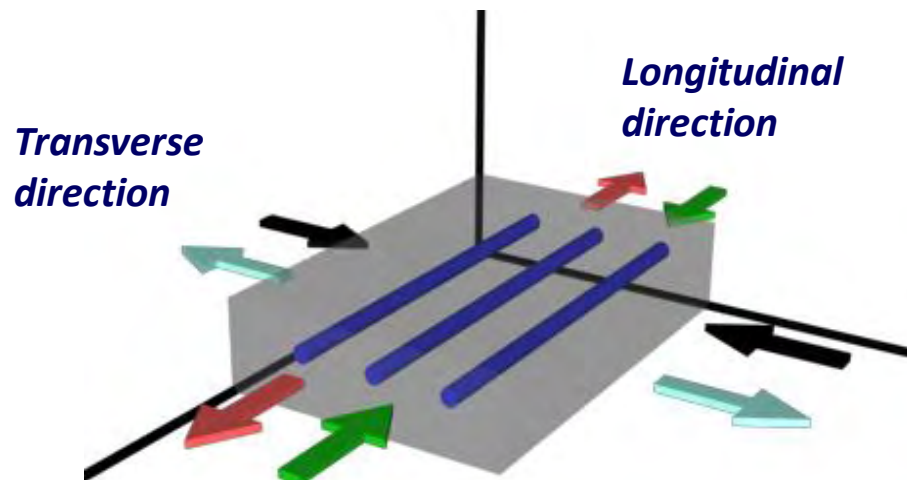


Performance of curved FRP's



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The tensile strength of FRP bars can be largely reduced when subjected to a biaxial state of stress



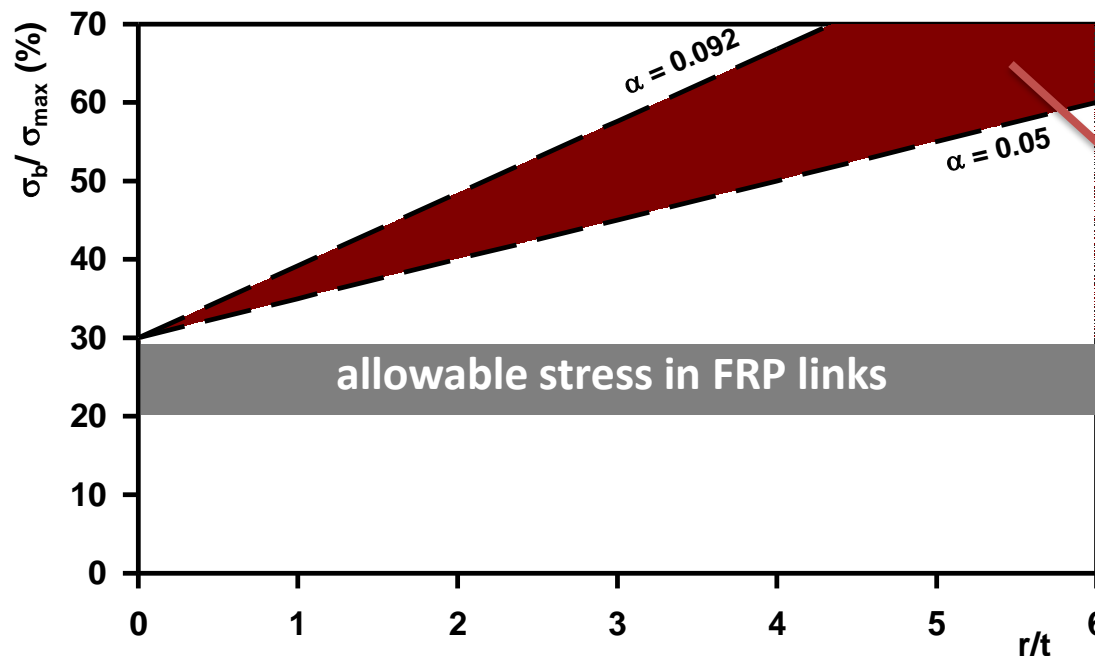
**Premature failure
at bent portion**

Code Provisions



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Design equation (JSCE)



$$f_{fb} = \left(\alpha \frac{r_b}{d_b} + 0.3 \right) f_{fu} \leq f_{fu}$$

r_b is the radius of the bend in the bar

d_b is the nominal diameter of the FRP bar

f_{fu} is the design strength of a straight portion of the bar

Code Provisions



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$$f_{fb} = \left(\alpha \frac{r_b}{d_b} + 0.3 \right) f_{fu} \leq f_{fu}$$

Bend geometry

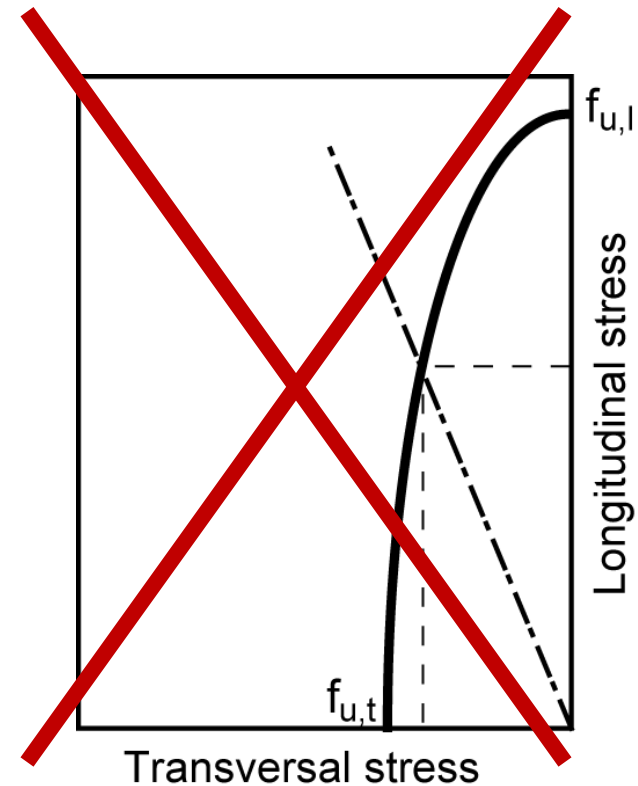
- r/t

~~Composite make-up~~

~~- type of fibres~~

~~- type of resin~~

~~- volume fractions~~



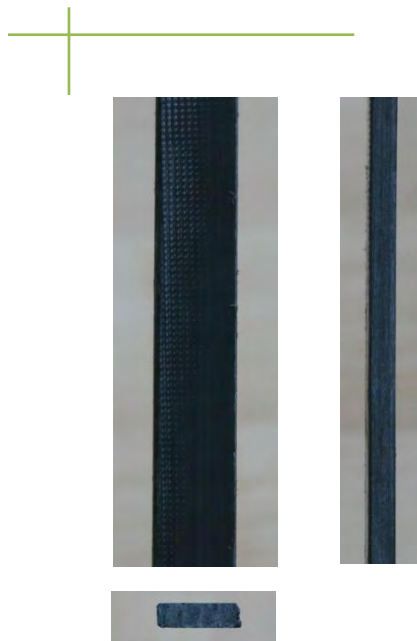
Experimental Programme



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GFRP thermoplastic strip (10x3mm)



Properties

Tensile strength (MPa)	720
Tensile modulus (GPa)	28
Ultimate strain (%)	1.9
Glass content (%v/v)	35
Density (g/cm ³)	1.48

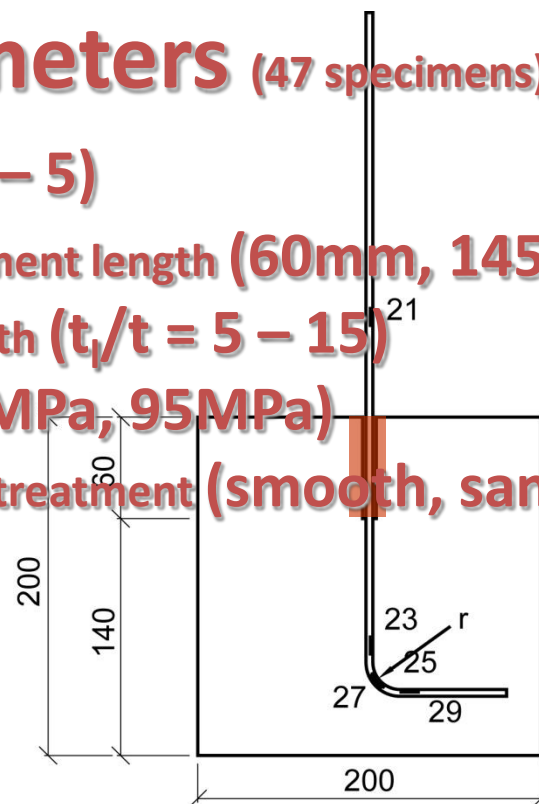
Experimental Programme



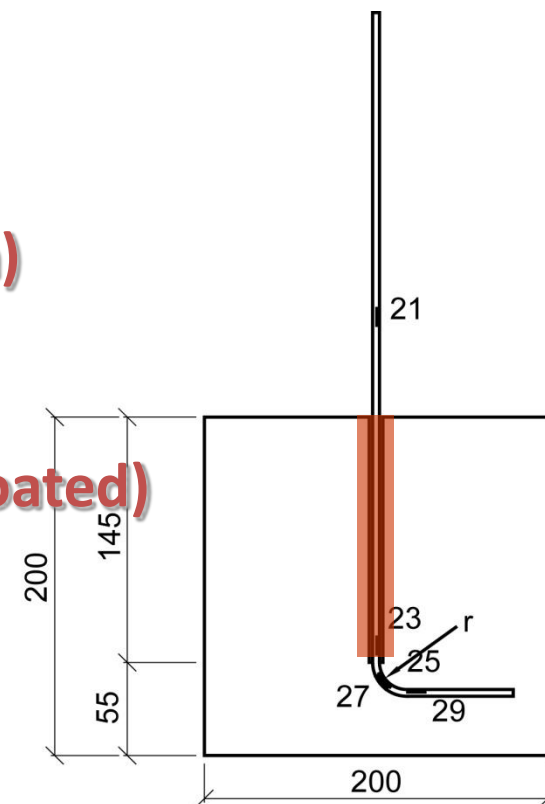
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Parameters (47 specimens)

- R/t (2 – 5)
- embedment length (60mm, 145mm)
- tail length ($t_1/t = 5 - 15$)
- f_{cu} (45MPa, 95MPa)
- surface treatment (smooth, sand coated)



Type 2

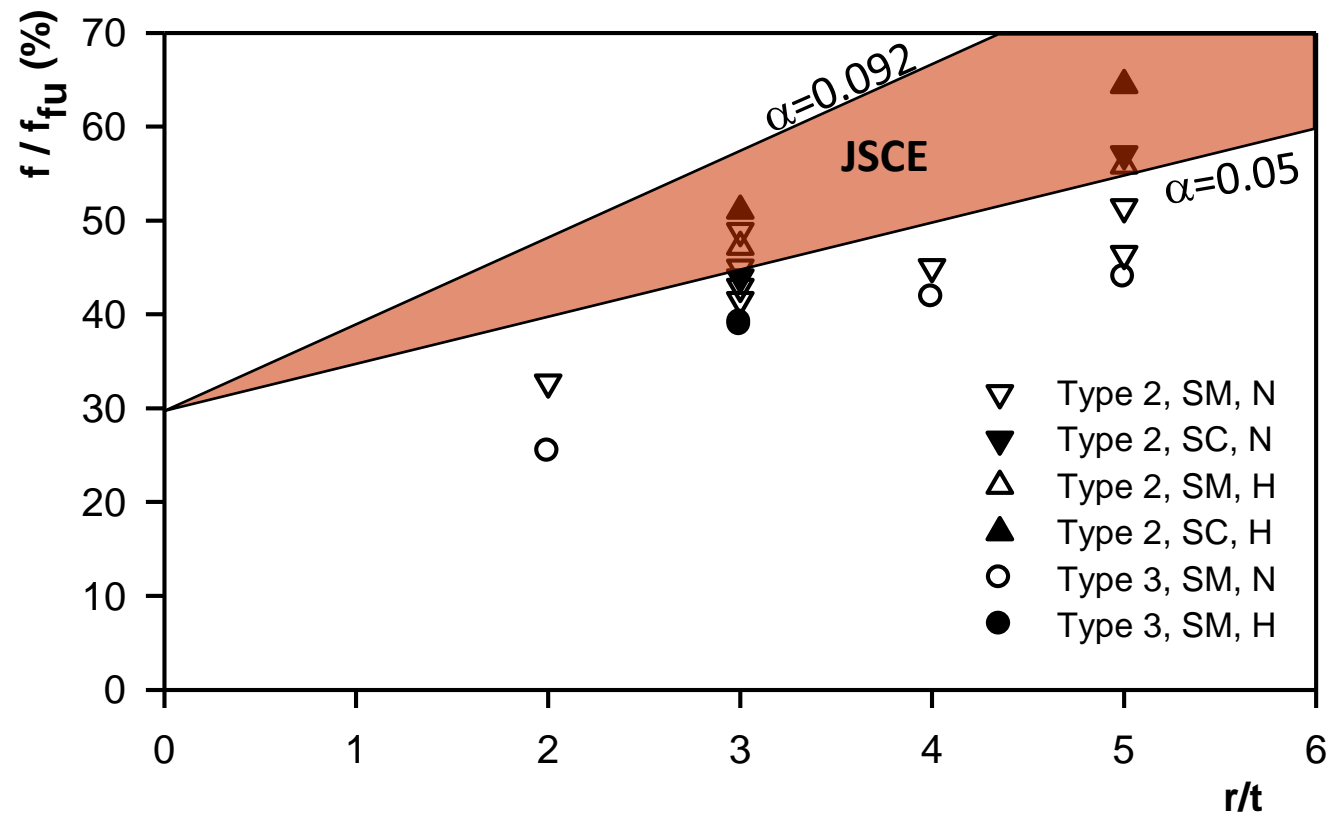


Type 3

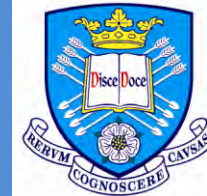
Experimental Results



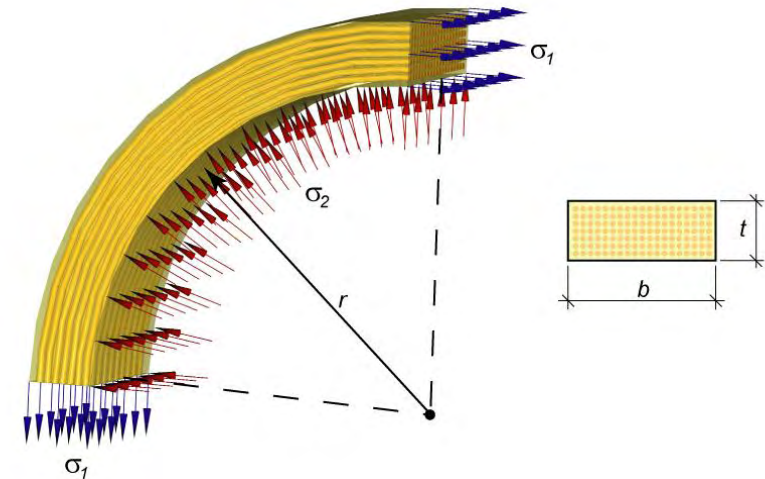
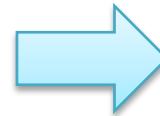
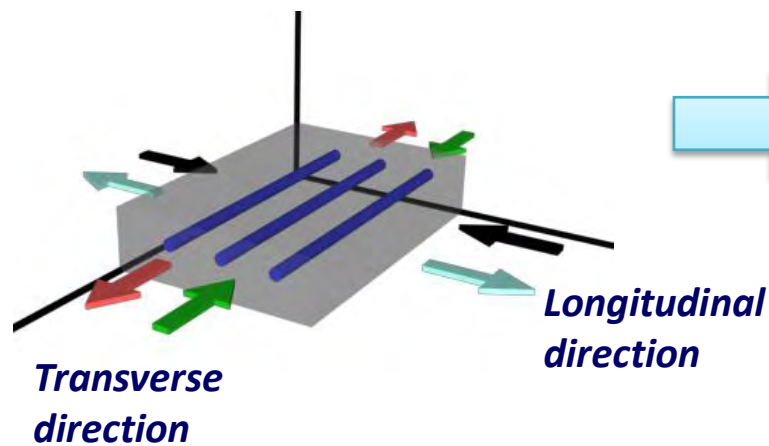
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A macromechanical approach



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• Force equilibrium

$$\sigma_2 = \sigma_1 \frac{t}{r}$$

• Failure criterion

$$\frac{\sigma_1^2}{\sigma_{1,\max}^2} - \frac{\sigma_1 \sigma_2}{\sigma_{1,\max}^2} + \frac{\sigma_2^2}{\sigma_{2,\max}^2} = 1$$

A macromechanical approach



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• Predictive model

$$\frac{\sigma_1}{\sigma_{1,\max}} = \frac{1}{\sqrt{1 + \left(\frac{h}{R}\right) + \left(\frac{h}{R}\right)^2 \cdot \beta^2}}$$

• Material testing

• Micromechanics

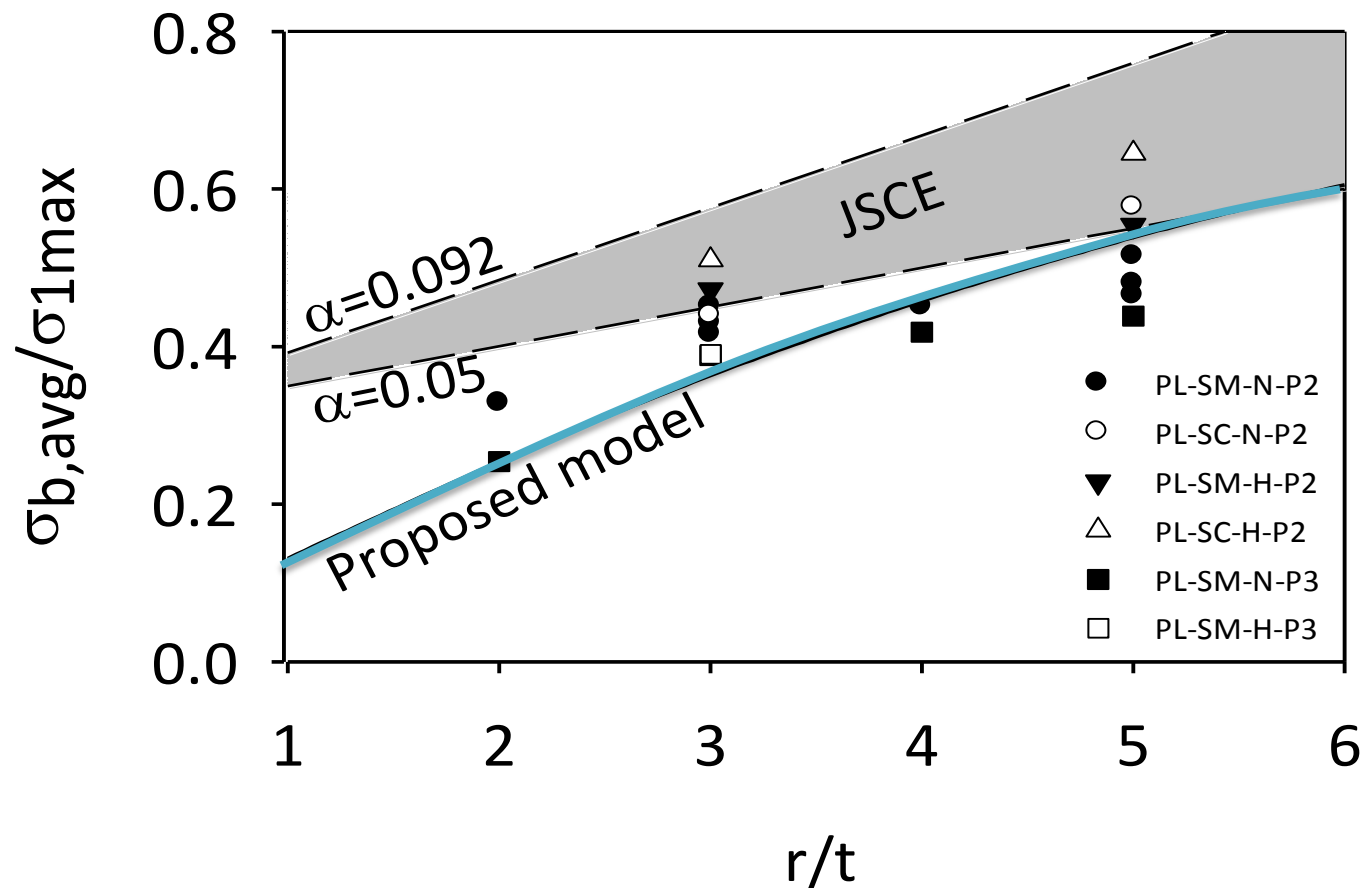
$$\sigma_{2,\max} = \frac{1}{k_\sigma} (f_{mc} + \sigma_{rm})$$

$$\beta = \frac{\sigma_{1,\max}}{\sigma_{2,\max}}$$

A macromechanical approach



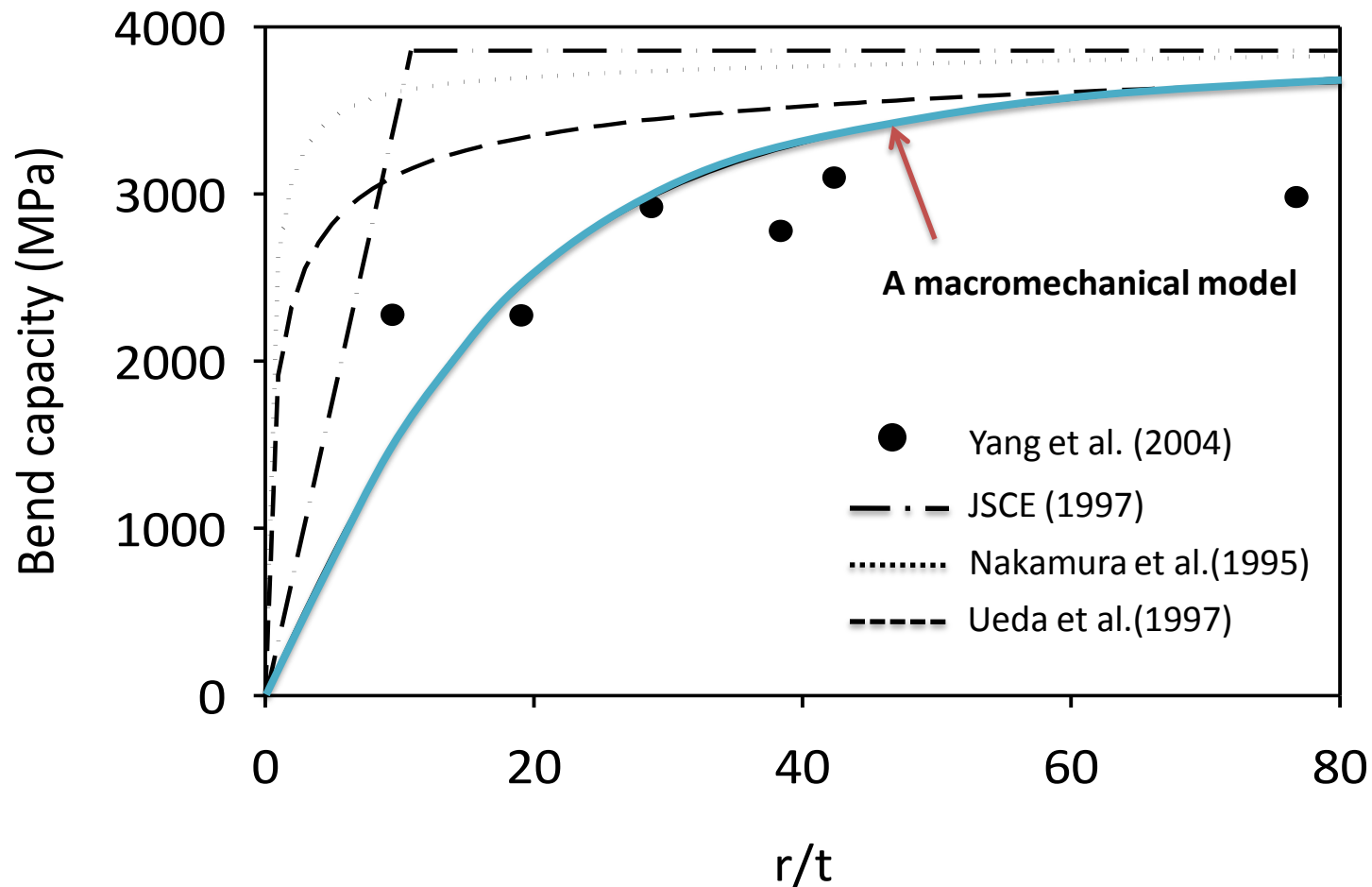
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Verifications



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Concluding Remarks



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- **The capacity of the bent portion is not only a function of its geometry**
- **Values of $r/t > 3-4$ guarantee the development of 40% of the ultimate strength**
- **The macromechanical based model adequately captures strength degradation of bent bars**